

3472/2
ADDITIONAL
MATHEMATICS
Kertas 2
Ogos 2017
2 ½ hours

PENILAIAN PERCUBAAN SPM NEGERI PAHANG 2017

ADDITIONAL MATHEMATICS

PERATURAN PERMARKAHAN

Kertas 2

| No | Solution | Sub Mark | Total |
|-----------|-----------------------------------------------------------------------------------------------------|----------|-------|
| 1(a) | $x^2 - \left(\frac{2}{m} + 1\right)x + \frac{3n - 1}{m} = 0$ | 1 | 7 |
| | $n + \frac{1}{m} = \frac{2}{m} + 1$ (S.O.R/H.T.P) OR $\frac{n}{m} = \frac{3n - 1}{m}$ (P.O.R/H.D.P) | 1 | |
| | $n = 3n - 1$ OR other method of simultaneous equation | 1 | |
| | $m = -2$ | 1 | |
| | $n = \frac{1}{2}$ | 1 | |
| 1 (b) | 3 (S.O.R/H.T.P) OR 2 (P.O.R/H.D.P) | 1 | 6 |
| | $x^2 - 3x + 2 = 0$ | 1 | |
| 2 (a) | $\sqrt{\frac{75\,019\,200}{12}} - \left(\frac{30\,000}{12}\right)^2, N = 12$ | 1 | |
| | $\bar{X} = 2\,500$ | 1 | |
| | $\sigma = 40$ | 1 | |
| 2 (b) | $\bar{X} = 2\,500 + 2\,500$ | 1 | |
| | $\bar{X} = 5\,000$ | 1 | |
| | $\sigma = 40$ | 1 | |
| 3 (a) | Use $\text{cosec } x = 1 + \cot^2 x$ | 1 | 8 |
| | Use $1 - 2 \sin^2 x = \cos 2x$ | 1 | |
| 3 (b) (i) | | | |
| | Shape of $\cos x$ graph | 1 | |
| | 2 cycles for $0 \leq x \leq 2\pi$ | 1 | |
| | Max = 4 and min = 2, Extension +3 | 1 | |
| | Reflection | 1 | |

| 3 (b) (ii) | $-5a + 3 = 4$ | 1 | | | | | | | | | | | | | | | | | | | |
|---------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|------|------|------|------|---|----|---|----|---------------|------|------|------|------|------|------|--|--|--|--|
| | $a = -\frac{1}{5}$ | 1 | | | | | | | | | | | | | | | | | | | |
| 4 | $4pq + \pi p^2 = 240\pi$ (non linear) | 1 | 6 | | | | | | | | | | | | | | | | | | |
| | $q = \frac{p}{2}\pi + 2\pi$ (linear) | 1 | | | | | | | | | | | | | | | | | | | |
| | $4p\left(\frac{p}{2}\pi + 2\pi\right) + \pi p^2 = 240\pi$ (eliminate q) | 1 | | | | | | | | | | | | | | | | | | | |
| | $p = \frac{-8 \pm \sqrt{(-8)^2 - 4(3)(-240)}}{2(3)}$ | 1 | | | | | | | | | | | | | | | | | | | |
| | $p = 7.71 \text{ cm}$ | 1 | | | | | | | | | | | | | | | | | | | |
| | $q = 18.40 \text{ cm}$ | 1 | | | | | | | | | | | | | | | | | | | |
| 5 (a) | $2x^2h = 72$ $h = \frac{36}{x^2}$ | 1 | 6 | | | | | | | | | | | | | | | | | | |
| | $L = 4x^2 + 6xh$ | 1 | | | | | | | | | | | | | | | | | | | |
| | $L = 4x^2 + 6x\left(\frac{36}{x^2}\right)$ $L = 4x^2 + \frac{216}{x}$ (shown) | 1 | | | | | | | | | | | | | | | | | | | |
| 5 (b) | $8x - \frac{216}{x^2} = 0$ | 1 | | | | | | | | | | | | | | | | | | | |
| | $x = 3$ | 1 | | | | | | | | | | | | | | | | | | | |
| | $L = 108 \text{ cm}^2$ | 1 | | | | | | | | | | | | | | | | | | | |
| 6 (a) | $\overrightarrow{OA} + \overrightarrow{AB} = 9\underline{i} + 15\underline{j}$ | 1 | 7 | | | | | | | | | | | | | | | | | | |
| | $ \overrightarrow{OB} = \sqrt{9^2 + 15^2}$ | 1 | | | | | | | | | | | | | | | | | | | |
| | Unit vector in the direction $\overrightarrow{OB} = \frac{1}{\sqrt{34}}(3\underline{i} + 5\underline{j})$ (can be implied) | 1 | | | | | | | | | | | | | | | | | | | |
| 6 (b) | $\overrightarrow{CA} = -\underline{i} - 9\underline{j}$ | 1 | | | | | | | | | | | | | | | | | | | |
| | $\overrightarrow{CE} = \underline{i} - 6\underline{j}$ | 1 | | | | | | | | | | | | | | | | | | | |
| | $\overrightarrow{CE} = \overrightarrow{CA} + \overrightarrow{AE}$ | 1 | | | | | | | | | | | | | | | | | | | |
| | $\overrightarrow{CE} \neq k \overrightarrow{OC}$ | 1 | | | | | | | | | | | | | | | | | | | |
| 7 (a) | <table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: center;">x</th><th style="text-align: center;">1</th><th style="text-align: center;">2</th><th style="text-align: center;">3</th><th style="text-align: center;">4</th><th style="text-align: center;">5</th><th style="text-align: center;">6</th><th rowspan="2" style="text-align: center; vertical-align: middle;">1</th><th rowspan="2" style="text-align: center; vertical-align: middle;">10</th></tr> </thead> <tbody> <tr> <td style="text-align: center;">$\frac{1}{y}$</td><td style="text-align: center;">0.46</td><td style="text-align: center;">0.39</td><td style="text-align: center;">0.30</td><td style="text-align: center;">0.22</td><td style="text-align: center;">0.15</td><td style="text-align: center;">0.07</td><td></td><td></td></tr> </tbody> </table> | x | 1 | 2 | 3 | 4 | 5 | 6 | 1 | 10 | $\frac{1}{y}$ | 0.46 | 0.39 | 0.30 | 0.22 | 0.15 | 0.07 | | | | |
| x | 1 | 2 | 3 | 4 | 5 | 6 | 1 | 10 | | | | | | | | | | | | | |
| $\frac{1}{y}$ | 0.46 | 0.39 | 0.30 | 0.22 | 0.15 | 0.07 | | | | | | | | | | | | | | | |

| | | | |
|-------|--------------------------------------------------------------------------------------------------------------------|---|----|
| | Plot $\frac{1}{y}$ against x and correct axes and uniform scales (pg 9) | 1 | |
| | 6 points plotted correctly | 1 | |
| | Line of best fit (Attachment, pg 9.) | 1 | |
| 7 (b) | $\frac{1}{y} = \frac{r}{3}x + 2s$ can be implied | 1 | |
| | $\frac{1}{y} = 0.25$ | 1 | |
| | $y = 4$ | 1 | |
| | Gradient, $\frac{r}{3} = \frac{0.56-1}{0-7}$ | 1 | |
| | $r = -0.24$ | 1 | |
| | $s = 0.28$ | 1 | |
| 8(a) | $\frac{dy}{dx} = 2x - 6 = 0$ | 1 | |
| | P(3, 1) | 1 | |
| 8(b) | $5x^2 = x^2 - 6x + 10$ solve simultaneous equation | 1 | |
| | $(2x + 5)(x - 1) = 0$ | 1 | |
| | Q(1, 5) | 1 | |
| 8(c) | $\left[\frac{5x^3}{3} \right]_0^1$ or $\left[\frac{x^3}{3} - 3x^2 + 10x \right]_1^3$ | 1 | |
| | $\frac{5(1)^3}{3} + \left(\frac{3^3}{3} - 3(3)^2 + 10(3) \right) - \left(\frac{1^3}{3} - 3(1)^2 + 10(1) \right)$ | 1 | |
| | $6\frac{1}{3}$ | 1 | |
| 8(d) | $\pi \left[\frac{25x^5}{5} \right]_0^1$ | 1 | |
| | 5π | 1 | 10 |

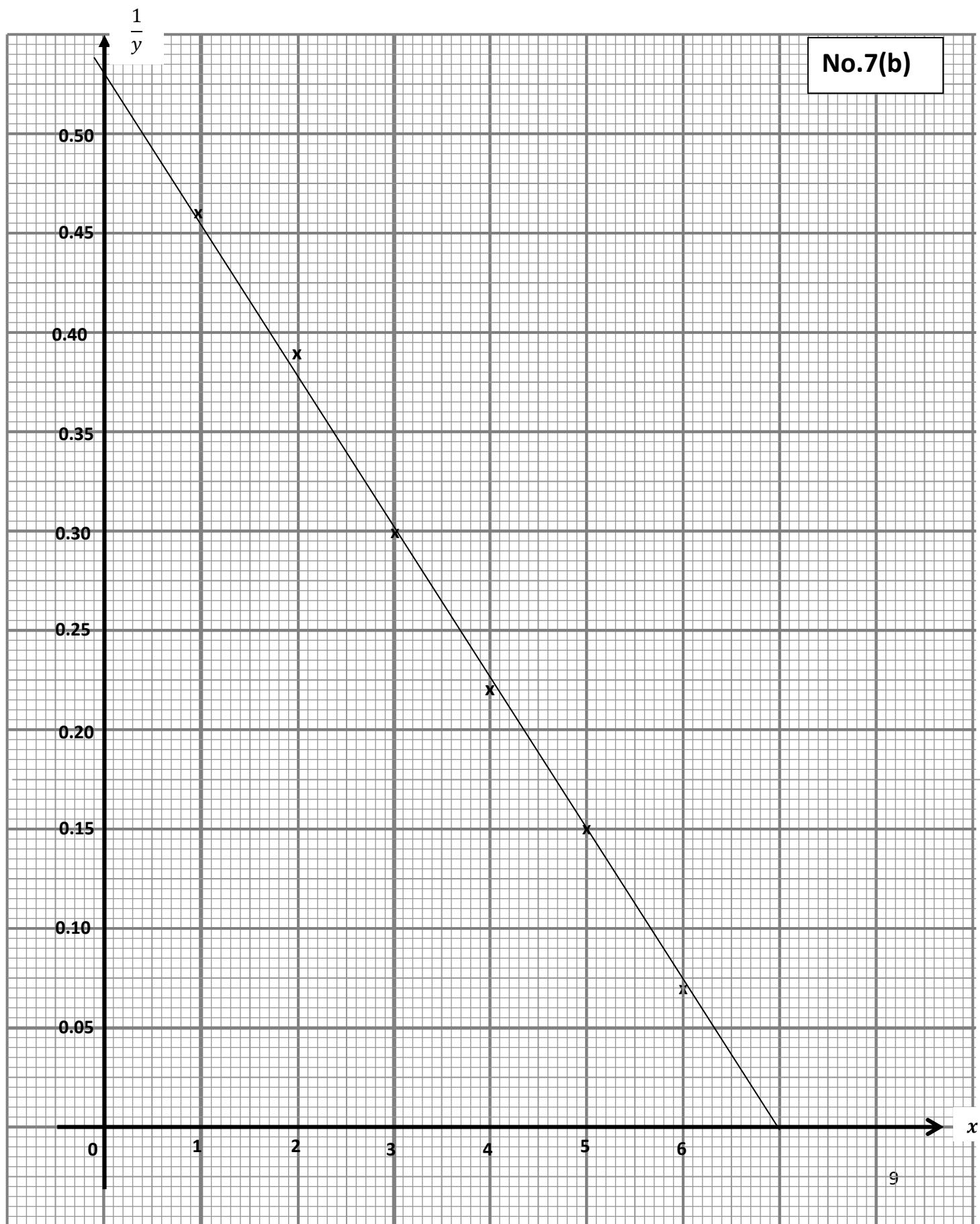
| | | | |
|-----------|--------------------------------------------------------------------------------------------------------------------|---|----|
| 9(a) | $\sin \angle POQ = \frac{12}{15}$ | 1 | |
| | $\angle POQ = 1.855 \text{ rad}$ | | |
| 9(b) | $15(1.855)$ | 1 | |
| | $12(3.142)$ | 1 | |
| | $15(1.855) + 12(3.142) + 20 + 11 + 11$ | 1 | |
| | 107.5 | 1 | |
| 9(c) | $\frac{1}{2}(3.142)(12)^2$ | 1 | 10 |
| | $\frac{1}{2}(15)^2(1.855) \text{ or } \frac{1}{2}(15)^2 \sin 106.26$ | 1 | |
| | $\frac{1}{2}(3.142)(12)^2 - [\frac{1}{2}(15)^2(1.855) - \frac{1}{2}(15)^2 \sin 106.26] + \frac{1}{2}(1.818)(11)^2$ | 1 | |
| | 235.5 | 1 | |
| | | | |
| 10(a)(i) | $7C_5(0.4)^5(0.6)^2 \text{ or } 7C_6(0.4)^6(0.6)^1 \text{ or } 7C_7(0.4)^7(0.6)^0$ | 1 | |
| | $1 - 7C_5(0.4)^5(0.6)^2 - 7C_6(0.4)^6(0.6)^1 - 7C_7(0.4)^7(0.6)^0$ | 1 | |
| | 0.9037 | 1 | |
| 10(a)(ii) | $1000(0.4) = 400$ | 1 | |
| | $\sqrt{1000(0.4)(0.6)} = 15.49$ | 1 | |
| 10(b)(i) | $\frac{7.5 - \mu}{0.5} = 1.0$ | 1 | 10 |
| | 7 | 1 | |
| 10(b)(ii) | $\frac{6.2 - 7}{0.5} \text{ or } \frac{6.4 - 7}{0.5}$ | 1 | |
| | 0.0603 | 1 | |
| | $0.0603 \times 4000 = 241$ | 1 | |
| | | | |

| | | | |
|-------|-------------------------------------------------------------------------------|---|----|
| | $m_{PR} = -\frac{3}{2}$ | 1 | |
| 11(a) | $y - 2 = -\frac{3}{2}(x - 16)$ | 1 | |
| | $y = -\frac{3}{2}x + 26$ | 1 | |
| | $\frac{2}{3}x = -\frac{3}{2}x + 26$ solve simultaneous equation | 1 | |
| 11(b) | $x = 12$ | 1 | |
| | R (12, 8) | 1 | |
| 11(c) | $\frac{1}{2} 0 + 24 + 0 - 0 - 128 - 0 $ | 1 | |
| | 52 | 1 | |
| | $\sqrt{(x - 12)^2 + (y - 8)^2} = 150$ | 1 | |
| | $x^2 + y^2 - 24x - 16y - 22292 = 0$ | 1 | 10 |
| 12(a) | $130 = \frac{p_{2014}}{500} \times 100$ | 1 | |
| | RM650 | 1 | |
| 12(b) | $\frac{130(120) + 110(100) + 105(35) + 115(35) + 120(70)}{360}$ | 2 | |
| | 118.61 | 1 | |
| | The monthly expenses increased 18.61% in the year 2014 based on the year 2010 | 1 | |
| 12(c) | $118.61 = \frac{3000}{p_{2010}} \times 100$ | 1 | |
| | RM 2529.30 | 1 | |
| 12(d) | $118.61 \times \frac{112}{100}$ | 1 | 10 |
| | 132.84 | 1 | |

| | | | |
|-----------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---|----|
| 13(a)(i) | $ST = 15$ | 1 | |
| 13(a)(ii) | $PT^2 = 9^2 + 15^2 - 2(9)(15) \cos 50$ | 1 | |
| | 11.51 | 1 | |
| 13(b) | $\frac{\sin \theta}{9} = \frac{\sin 50}{11.51}$ | 1 | |
| | 36.80^0 | 1 | |
| 13(c) | $\frac{1}{2}(9)(15) \sin 50$ | 1 | |
| | 51.71 | 1 | |
| 13(d) | $\frac{1}{2}(h)(15) = 51.71 \quad h = 6.895$ | 1 | |
| | $\frac{1}{3} \times \left(\frac{1}{2}(16)(15)\right) \times 6.895$ | 1 | |
| | 275.8 | 1 | 10 |
| 14(a) | 10 | 1 | |
| 14(b) | $\left(\frac{7}{2}\right)^2 - 7\left(\frac{7}{2}\right) + 10 \text{ or } \left(t - \frac{7}{2}\right)^2 - \frac{9}{4}$ | 1 | |
| | $q = -\frac{9}{4}$ | 1 | |
| | q represents the minimum velocity of the particle | 1 | |
| 14(c) | $a = 2t - 7$ | 1 | |
| | $[2(3) - 7] - [2(2) - 7]$ | 1 | |
| | 2 | 1 | |
| 14(d) | $\left[\frac{t^3}{3} - \frac{7t^2}{2} + 10t\right]_0^2 \text{ or } \left \left[\frac{t^3}{3} - \frac{7t^2}{2} + 10t\right]_2^5\right $ | 1 | |
| | $\left[\frac{2^3}{3} - \frac{7(2)^2}{2} + 10(2) - 0\right] + \left \left[\frac{5^3}{3} - \frac{7(5)^2}{2} + 10(5)\right] - \left[\frac{2^3}{3} - \frac{7(2)^2}{2} + 10(2)\right]\right $ | 1 | |
| | $13\frac{1}{6}$ | 1 | 10 |

| | | | |
|-----------|----------------------------------------------------------------------------------------------------|---|----|
| 15(a) | I $x + y \leq 80$ | 1 | |
| | II $y - x \leq 20$ | 1 | |
| | III $x \leq 3y$ | 1 | |
| 15(b) | Graph (Attachment, pg.10) | | |
| | At least one straight line is drawn correctly from the inequalities involving x and y . | 1 | |
| | All the straight lines are drawn correctly. | 1 | |
| | Region is shaded correctly. | 1 | |
| 15(c)(i) | $x_{max} = 45$ | 1 | |
| 15(c)(ii) | Maximum point = (60, 20) | 1 | 10 |
| | Maximum cost = $30(60) + 25(20)$ | 1 | |
| | RM 2300 | 1 | |

No.7(b)



y

No.14(b)

